# MATH-1620: CALCULUS II

## **Cuyahoga Community College**

## Viewing: MATH-1620 : Calculus II

Board of Trustees: November 2020

Academic Term: Fall 2021

Subject Code

MATH - Mathematics

#### Course Number:

1620

Title:

Calculus II

#### **Catalog Description:**

Second of three-semester sequence. Includes the study of applications of the definite integral, techniques of integration, indeterminate forms, improper integrals, sequences, series, conic sections, parametric equations and polar coordinates.

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Credit Hour(s):
5
Lecture Hour(s):
5
Lab Hour(s):
0
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Other Hour(s):

0

## **Requisites**

#### **Prerequisite and Corequisite**

MATH-1610 Calculus I, or departmental approval: equivalent coursework.

## Outcomes

## Course Outcome(s):

Apply definite integrals to solve geometric and STEM application problems.

## **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

## Objective(s):

- 1. Describe how Riemann sums are used to approximate solutions of geometric problems and lead to definite integrals.
- 2. Set up and evaluate definite integrals that represent the area between two curves.
- 3. Set up and evaluate definite integrals that represent the volume of solids of revolution.
- 4. Utilize definite integrals to calculate the arc length of curves.
- 5. Utilize definite integrals to calculate areas of surfaces of revolution.
- 6. Describe work as the limit of a Riemann sum and utilize definite integrals to solve work problems.

## Course Outcome(s):

Utilize a variety of techniques to evaluate integrals.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Perform integration by parts.
- 2. Evaluate trigonometric integrals using substitutions and identities.
- 3. Utilize trigonometric substitutions to evaluate integrals involving radicals and other functions.
- 4. Utilize the method of partial fractions to evaluate integrals involving rational functions.
- 5. Perform numerical integration using the Trapezoidal Rule and Simpson's Rule.
- 6. Recognize the appropriate rule or technique for evaluating a particular integral.
- 7. Utilize technology to evaluate integrals.

#### Course Outcome(s):

Evaluate limits of functions and improper integrals.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Identify indeterminate forms resulting from limits.
- 2. Apply L'Hôpital's Rule to evaluate limits.
- 3. Identify improper integrals.
- 4. Utilize limits to evaluate improper integrals.

#### Course Outcome(s):

Apply convergence tests to sequences and series, and solve application problems.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Distinguish between sequences and series.
- 2. Identify the *n*th-term of a sequence or series.
- 3. Utilize limits and graphs of sequences to determine convergence.
- 4. Find the *n*th partial sum of a series.
- 5. Identify special types of series including geometric series, telescoping series, alternating series, p-series and power series.
- 6. Determine the convergence of a series using various tests, including the *n*th term, geometric series, integral, *p*-series, comparison, alternating series, ratio, and root tests.
- 7. Create Taylor and Maclaurin polynomials to approximate functions.
- 8. Find the radius and interval of convergence of power series.
- 9. Perform mathematical operations on power series, such as addition, multiplication, integration and differentiation, to create power series for other functions.
- 10. Create Taylor and Maclaurin series for functions using the definition and by using power series for elementary functions.

#### Course Outcome(s):

Analyze functions and curves defined by parametric and polar equations.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Convert between parametric and rectangular equations.
- 2. Sketch curves defined by parametric equations, and indicate the orientation.
- 3. Plot points and curves in the polar coordinate system.

- 4. Convert rectangular coordinates and equations to polar form and vice versa.
- 5. Solve calculus problems involving parametric and polar equations.
- 6. Utilize technology to solve problems with functions expressed in parametric and polar form.

#### Methods of Evaluation:

- 1. Exams
- 2. Quizzes
- 3. Homework
- 4. Projects
- 5. Collaborative Work

#### **Course Content Outline:**

- 1. Applications of Definite Integrals
  - a. Area between two curves
  - b. Volume of solids of revolution
  - c. Arc length
  - d. Area of surfaces of revolution
  - e. Work
- 2. Integration Techniques
  - a. Integration by inspection
  - b. Integration by parts
  - c. Trigonometric integrals
  - d. Trigonometric substitution
  - e. Partial fractions
  - f. Numerical integration
- 3. Limits and Improper Integrals
  - a. Indeterminate forms
  - b. L'Hôpital's Rule
  - c. Improper integrals
- 4. Sequences and series
  - a. Graphs of sequences
  - b. Limits of sequences and convergence
  - c. The nth partial sum of a series
  - d. Convergence tests for series
    - i. The *n*th-term test
    - ii. Geometric series test
    - iii. Integral test
    - iv. The *p*-series test
    - v. Comparison tests
    - vi. Alternating series test
    - vii. Ratio and root tests
  - e. Taylor and Maclaurin polynomials
  - i. Local linear and quadratic approximations
  - f. Power series
    - i. Radius of convergence
    - ii. Interval of convergence
    - iii. Operations on power series
    - iv. Representation of functions with Taylor and Macluarin series
- 5. Conic sections
  - a. Parabolas
  - b. Ellipses
  - c. Hyperbolas
- 6. Parametric equations
  - a. Parameters
  - b. Graphs
  - c. Orientation

- d. Parametric equations of a curve
- e. Parametric form of the derivative
- 7. Polar Coordinates
  - a. Polar coordinate system
  - b. Conversion between polar and rectangular form
  - c. Graphs of polar equations
  - d. Slope in polar form
  - e. Area of polar curves

#### Resources

Larson, Ron; Edwards, Bruce. Calculus - Early Transcendental Functions. 9th Edition. Cengage , 2019.

Stewart, James; Clegg, Daniel; Watson, Saleem. Calculus - Early Transcendentals. 9th Edition. Cengage, 2021.

Briggs, William; Cochran, Lyle; Gillett, Bernard; Schulz, Eric. Calculus - Early Transcendentals. 3rd Edition. Pearson, 2019.

#### **Resources Other**

- 1. Textbook Software
- 2. Computer Algebra Systems: Maple, Mathematica, Derive and Converge

## **Instructional Services**

#### OAN Number:

Ohio Transfer 36 TMM006 and TMM017 (2 of 2 courses, both must be taken)

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