MATH-1530: College Algebra

# MATH-1530: COLLEGE ALGEBRA

# **Cuyahoga Community College**

Viewing: MATH-1530 : College Algebra

**Board of Trustees:** 

June 2022

**Academic Term:** 

Fall 2021

**Subject Code** 

MATH - Mathematics

Course Number:

1530

Title:

College Algebra

#### **Catalog Description:**

Topics include extensive function (linear, quadratic, polynomial, radical, roots, power, piece-wise, exponential, logarithmic) representation including verbal, numeric, graphic, and algebraic, identifying properties of the different function types, transformation of functions, solve linear, polynomial, rational, absolute value, exponential and logarithmic equations. Solve quadratic, polynomial and rational inequalities in one variable. Determine and graph conic sections, solve non-linear systems of equations and inequalities and solve systems of equations using matrices. Includes applications and activities to build skills in problem solving.

# Credit Hour(s):

4

# Lecture Hour(s):

4

# Requisites

#### **Prerequisite and Corequisite**

MATH-0965 Intermediate Algebra or qualified math placement; or departmental approval for equivalent coursework. Note: MATH-1200 or MATH-1280 taken prior to Fall 2016 or MATH-1270 taken prior to Summer 2017 will also be accepted to meet prerequisite requirements for this course.

# **Outcomes**

# Course Outcome(s):

Represent functions verbally, numerically, graphically and algebraically.

# **Essential Learning Outcome Mapping:**

Critical/Creative Thinking: Analyze, evaluate, and synthesize information in order to consider problems/ideas and transform them in innovative or imaginative ways.

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Define and identify relation, domain, range, and function.
- 2. Identify and perform transformations of functions.
- 3. Define, identify, and analyze linear, quadratic, polynomial, rational, root/radical/power and piece-wise functions algebraically and graphically, including the domain and range.
- 4. Determine the vertex of a quadratic function.
- 5. Identify and determine asymptotes of rational functions.
- 6. Sketch graphs of rational functions.
- 7. Determine exact and/or approximate zeros and sketch the graphs of polynomial functions of degree greater than two.
- 8. Use the Remainder Theorem and Factor Theorems for polynomial functions including the Fundamental Theorem of Algebra and the Rational Zero Theorem
- 9. Define and determine zeros or roots of a polynomial function including irrational and complex zeros, based on operations with complex numbers.

- 10. Determine intervals on which the function is increasing, decreasing or constant.
- 11. Determine algebraically and graphically whether the graph of an equation exhibits symmetry.
- 12. Use the vertical line test to identify functions.
- 13. Graph functions and their inverses.
- 14. Determine if a function is even or odd.
- 15. Identify and determine relative maximum and minimum values in an interval of a function.
- 16. Define exponential and logarithmic functions.
- 17. Determine the domain and ranges of exponential and logarithmic functions.
- 18. Graph exponential and logarithmic functions, using their properties.
- 19. Identify Properties of Logarithmic functions including the Product, Quotient, Power, and Change of Base Rules and use the properties to rewrite logarithmic functions.
- 20. Define and evaluate common and natural logarithms.
- 21. Use functions to model a variety of real-world problem-solving applications.
- 22. Use the horizontal line test to determine if a function is one-to-one.
- 23. Define and determine inverse functions algebraically.
- 24. Perform operations (sum, difference, product, and quotient) on functions and determine the domain of the resulting functions.
- 25. Divide a polynomial function by a linear function using synthetic division.
- 26. Divide a polynomial function by a polynomial function using long division.
- 27. Determine the composite of two functions and the domain of the composite function.
- 28. Decompose a function as a composite.
- 29. Choose and apply technology to assist in analyzing functions

#### Course Outcome(s):

Solve Equations.

# **Essential Learning Outcome Mapping:**

Critical/Creative Thinking: Analyze, evaluate, and synthesize information in order to consider problems/ideas and transform them in innovative or imaginative ways.

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

# Objective(s):

- 1. Apply the definition of absolute value to solve linear equations.
- 2. Use the one-to-one property of exponential functions to solve one-to-one exponential equations.
- 3. Use the Properties of Logarithms and the one-to-one property of logarithmic functions to solve one-to-one logarithmic equations.
- 4. Use the inverse relationship between the exponential function and logarithmic function to solve exponential and logarithmic equations.
- 5. Evaluate applications involving exponential and logarithmic functions and equations including exponential growth and decay and periodic and continuous compounding.

#### Course Outcome(s):

Solve inequalities.

#### **Essential Learning Outcome Mapping:**

Critical/Creative Thinking: Analyze, evaluate, and synthesize information in order to consider problems/ideas and transform them in innovative or imaginative ways.

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Apply the definition of absolute value to solve linear inequalities.
- 2. Solve quadratic, polynomial and rational inequalities in one variable.
- 3. Write the solution using set builder notation.
- 4. Write the solution using interval notation.
- 5. Graph the solution.
- 6. Apply the definition of absolute value to solve linear, polynomial, and rational absolute value inequalities.

#### Course Outcome(s):

Define, determine, and graph conic sections and solve non-linear systems of equations and inequalities.

#### **Essential Learning Outcome Mapping:**

Critical/Creative Thinking: Analyze, evaluate, and synthesize information in order to consider problems/ideas and transform them in innovative or imaginative ways.

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Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Define and use the distance and midpoint formulas.
- 2. Define and identify circles, ellipses, parabolas, and hyperbolas graphically.
- 3. Define and identify circles, ellipses, parabolas, and hyperbolas algebraically in standard and general forms.
- 4. Graph the conic sections centered at the origin and at the point (h, k) using the center, radius, major and minor axes, vertices, foci, directrix, axis of symmetry, and oblique asymptotes as necessary.
- 5. Solve systems of nonlinear equations using the substitution and elimination methods.
- 6. Solve systems of non-linear inequalities graphically
- 7. Solve real life application of conic sections including wheels, radar dish, support cables, and Earth's orbit.

#### Course Outcome(s):

Solve systems of linear equations using matrices.

# **Essential Learning Outcome Mapping:**

Critical/Creative Thinking: Analyze, evaluate, and synthesize information in order to consider problems/ideas and transform them in innovative or imaginative ways.

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- 1. Describe and use the basic properties of matrices.
- 2. Introduce Gaussian and Gauss-Jordan elimination methods.

#### Methods of Evaluation:

- 1. Exams
- 2. Quizzes
- 3. Homework
- 4. Online coursework
- 5. Projects
- 6. In-class collaborative work
- 7. Comprehensive final exam
- 8. Participation

# **Course Content Outline:**

- 1. Represent functions verbally, numerically, graphically and algebraically
  - a. Relation, domain, range, function
  - b. Vertical line test
  - c. Horizontal line test
  - d. Inverse functions
  - e. Sum, difference, product, and quotient of functions and their domain
  - f. Synthetic division
  - a. Long division
  - h. Composite of functions and the domain
  - i. Decompose a function as a composite
  - j. Transformations of functions
  - k. Linear, quadratic, polynomial, rational, root/radical/power and piece-wise functions, range and domain
  - I. Vertex of quadratic functions
  - m. Asymptotes of rational functions
  - n. Graphs of rational functions
  - o. Exact and/or approximate zeros and graphs of polynomial functions
  - p. Remainder Theorem and Factor Theorems, the Fundamental Theorem of Algebra and Rational Zero Theorem
  - q. Zeros or roots of a polynomial function, irrational and complex zeros using operations with complex numbers
  - r. Increasing, decreasing, constant intervals of functions
  - s. Symmetry algebraically and graphically
  - t. Graph functions and inverses

- u. Even or odd functions
- v. Relative maximum and minimum values in an interval of a function
- w. Exponential and logarithmic function definition
- x. Domain and range of exponential and logarithmic function
- y. Graphs, properties of exponential and logarithmic functions
- z. Properties of logarithmic functions including the Product, Quotient, Power, and Change of Base Rules and use these properties to rewrite logarithmic functions
- aa. Common and natural logarithms
- bb. Functions to model a variety of real-world problem-solving applications
- cc. Students choose and apply technology to assist in analyzing functions
- 2. Solve equations
  - a. Solve absolute value equations
  - b. One-to-one property of exponential functions to solve one-to-one exponential equations
  - c. One-to-one property of logarithmic functions to solve one-to-one logarithmic equations
  - d. Inverse relationship of exponential and logarithmic function to solve exponential and logarithmic functions
  - e. Applications of exponential and logarithmic functions and equations including exponential growth and decay and periodic and continuous compounding
- 3. Solve inequalities
  - a. Absolute value, quadratic, polynomial and rational inequalities in one variable
  - b. Set builder notation with inequalities
  - c. Interval notation with inequalities
  - d. Graph solutions of inequalities
  - e. Solve linear, polynomial, and rational absolute value inequalities
  - f. Set builder notation with absolute value inequalities
  - g. Interval notation with absolute value inequalities
  - h. Graph solutions with absolute value inequalities
- 4. Graph conic sections and solve non-linear systems of equations and inequalities
  - a. Distance and midpoint formulas
  - b. Circles, ellipses, parabolas, and hyperbolas graphically
  - c. Circles, ellipses, parabolas, and hyperbolas algebraically
  - d. Graph the conic sections centered at the origin and at the point (h, k) using the center, radius, major and minor axes, vertices, foci, directrix, axis of symmetry, and oblique asymptotes
  - e. Substitution and elimination methods to solve systems of nonlinear equations
  - f. Graphing to solve systems of non-linear inequalities
  - g. Real life application of conic sections including wheels, radar dish, support cables, and Earth's orbit
- 5. Systems of equations using matrices
  - a. Basic properties of matrices
  - b. Introduce Gaussian and Gauss-Jordan elimination methods

# Resources

Robert Blitzer. Precalculus. 6th. Boston, MA: Pearson Education, 2018.

Beecher, Penna, Bittinger. Algebra Trigonometry. 5th. Boston, MA: Pearson Education, 2016.

Sullivan. Algebra & Trigonometry. 11th. Boston, MA: Pearson Education, 2020.

#### **Resources Other**

- 1. Software provided through the publisher corresponding to the textbook
- 2. Software and E-book
- 3. TI-83 or TI-84 graphing calculator

# **Instructional Services**

#### **OAN Number:**

Ohio Transfer 36 TMM001 College Algebra and TMM002 Precalculus (1 of 2 courses, both MATH-1530 and MATH-1540 must be taken to meet TMM002)

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